

Reg No.: \_\_\_\_\_

Name: \_\_\_\_\_

**APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY**  
**FIFTH SEMESTER B.TECH DEGREE EXAMINATION(R&S), DECEMBER 2019**

**Course Code: EC301**

**Course Name: DIGITAL SIGNAL PROCESSING**

Max. Marks: 100

Duration: 3 Hours

**PART A**

*Answer any two full questions, each carries 15 marks.*

Marks

- 1 a) State Parseval's theorem of DFT? Using DFT find the energy of the sequence  $x(n) = 0.2^n u(n), n < 4$ . (7)
- b) Compute 8-point DFT of the sequence  $x(n) = \{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 0, 0, 0, 0\}$  using DITFFT algorithm. Follow exactly the corresponding flow graphs and keep track of all the intermediate quantities by putting them on diagram. (8)
- 2 a) Find linear convolution of the sequences  $x(n)$  and  $z(n)$  using circular convolution. Given  $x(n) = \{1, 2, 3, 1\}$  and  $z(n) = \{4, 3, 2\}$ . (7)
- b) Explain how N point DFTs of two real sequences can be found using by computing a single DFT. Illustrate with the sequences  $x_1(n) = \{4, 3, -1, 5\}$  and  $x_2(n) = \{6, -4, 2, 5\}$ . (8)
- 3 a) Find the number of real multiplications and additions involved in the computation of 64-point DFT using i) direct computation ii) FFT algorithm. Also comment on the computational advantage of FFT algorithm over the direct method. (7)
- b) Using Overlap Add method, find the output of the filter with filter response  $h(n)$  when an input  $x(n) = \{1, 2, 2, 3, 4, 2, 2, 1, 1\}$  is given. Take data block size of length  $L = 3$  and  $h(n) = \{2, 3, 4\}$ . (8)

**PART B**

*Answer any two full questions, each carries 15 marks.*

- 4 a) Design a linear phase FIR low pass filter with cut off frequency of 2 kHz and sampling rate of 8 kHz with a filter length 11 using Hanning window. (10)
- b) Find the filter transfer function  $H(z)$  from the analog filter with system function  $H(s)$  using Impulse Invariance method. (5)

$$H(s) = \frac{s + 1}{s^2 + 0.2s + 16.01}$$

- 5 a) Apply frequency sampling technique to design a linear phase FIR filter of length  $N=7$  with following specification. (10)

$$H_d(e^{j\omega}) = e^{-j\alpha\omega}; \quad 0 \leq |\omega| \leq 0.55\pi$$

$$= 0 \quad \text{otherwise}$$

- b) Transform the prototype low pass filter with system function  $H(s) = \frac{\Omega_c}{s + \Omega_c}$  (5)  
into high pass and band pass filters.
- 6 a) Design a Butterworth low pass digital IIR filter with a pass band edge frequency of  $0.25\pi$  with a ripple not exceeding **0.5 dB** and a minimum stop band attenuation **15dB** with a stop band edge frequency of  $0.55\pi$ . Use bilinear transformation. (10)
- b) Compare the performance of FIR filter design using rectangular window and Hamming window. (5)

### PART C

*Answer any two full questions, each carries 20 marks.*

- 7 a) Determine a direct form realization of the FIR filter with the following filter function using minimum number of multipliers. (4)  
 $h(n) = \{1, 2, 3, 4, 3, 2, 1\}$
- b) Draw the cascade and parallel form realisation of the filter with following transfer function (8)

$$H(z) = \frac{3(5 - 2z^{-1})}{\left(1 + \frac{1}{2}z^{-1}\right)(3 - z^{-1})}$$

- c) How upsampling and downsampling by a factor of 3 affect the frequency spectrum of a signal  $x(n)$  with frequency spectrum  $X(e^{j\omega})$ ? What is the need of low pass filter prior to downsampling? (8)
- 8 a) For the signal  $x(n) = 0.2^n u(n), n \leq 8$ , plot the following signals (4)  
(i)  $x(n)$  downsampled by 3 (ii)  $x(n)$  upsampled by 3
- b) With an example illustrate the error introduced by truncation and rounding in fixed point representation of numbers. (8)
- c) What is the effect of coefficient quantization in IIR filter structures? (8)
- 9 a) Obtain the direct form II, cascade and transposed direct form II structures for the (10)

system.

$$y(n) = -0.1y(n-1) + 0.2y(n-2) + 3x(n) + 3.6x(n-1) + 0.6x(n-2)$$

- b) Explain the architecture of TMS320C67xx DSP with block diagram. (10)

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